Core Mathematics C2 Paper L

Sketch on the same diagram the graphs of $y = \sin 2x$ and $y = \tan \frac{x}{2}$ for x 1. (i) in the interval $0 \le x \le 360^\circ$.

Hence state how many solutions exist to the equation *(ii)*

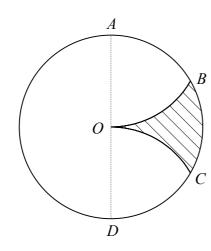
$$\sin 2x = \tan \frac{x}{2},$$

for x in the interval $0 \le x \le 360^\circ$ and give a reason for your answer.

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[4]

[2]



The diagram shows a circle of radius r and centre O in which AD is a diameter.

The points B and C lie on the circle such that OB and OC are arcs of circles of radius r with centres A and D respectively.

Show that the area of the shaded region *OBC* is
$$\frac{1}{6}r^2(3\sqrt{3}-\pi)$$
. [6]

3. The sequence u_1, u_2, u_3, \dots is defined by

$$u_{n+1} = (u_n)^2 - 1, n \ge 1.$$

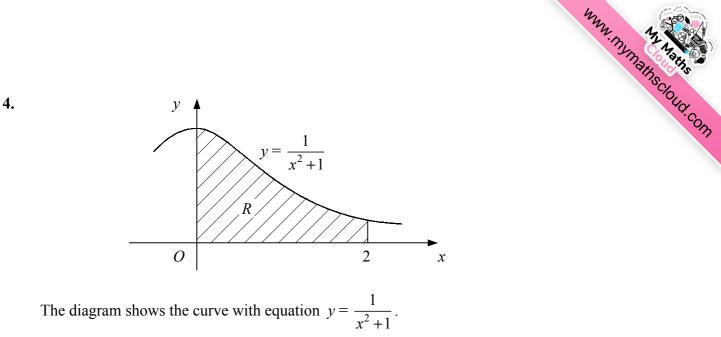
Given that $u_1 = k$, where k is a constant,

find expressions for u_2 and u_3 in terms of k. [3] (i)

Given also that $u_2 + u_3 = 11$,

(ii) find the possible values of *k*. [4]

2.



The shaded region *R* is bounded by the curve, the coordinate axes and the line x = 2.

(i) Use the trapezium rule with four strips of equal width to estimate the area of R. [5]

The cross-section of a support for a bookshelf is modelled by R with 1 unit on each axis representing 8 cm. Given that the support is 2 cm thick,

- (*ii*) find an estimate for the volume of the support. [2]
- 5. (i) Find the value of a such that

$$\log_a 27 = 3 + \log_a 8.$$
 [3]

(ii) Solve the equation

$$2^{x+3} = 6^{x-1},$$

giving your answer to 3 significant figures. [4]

6. (i) Evaluate

$$\int_{2}^{4} \left(2 - \frac{1}{x^{2}}\right) \, \mathrm{d}x.$$
 [4]

(ii) Given that

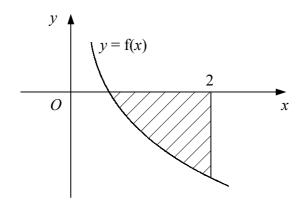
$$\frac{\mathrm{d}y}{\mathrm{d}x} = 2x^3 + 1$$

and that y = 3 when x = 0, find the value of y when x = 2. [5]

Turn over



[3]



The diagram shows part of the curve y = f(x) where $f(x) = \frac{1 - 8x^3}{x^2}$, $x \neq 0$.

- (*i*) Solve the equation f(x) = 0.
- (*ii*) Find $\int f(x) dx$. [3]
- (*iii*) Find the area of the shaded region bounded by the curve y = f(x), the x-axis and the line x = 2. [3]
- 8. A store begins to stock a new range of DVD players and achieves sales of £1500 of these products during the first month. In a model it is assumed that sales will decrease by $\pounds x$ in each subsequent month, forming an arithmetic sequence.

Given that sales total £8100 during the first six months, use the model to

- (i) find the value of x, [4]
- (*ii*) find the expected value of sales in the eighth month, [2]
- (*iii*) show that the expected total of sales in pounds during the first n months is given by kn(51 n), where k is an integer to be found. [3]
- *(iv)* Explain why this model cannot be valid over a long period of time. [1]
- 9.

 $f(x) = 2x^3 - 5x^2 + x + 2.$

(*i*) Show that
$$(x - 2)$$
 is a factor of $f(x)$. [2]

- (*ii*) Fully factorise f(x). [4]
- (*iii*) Solve the equation f(x) = 0. [1]
- (*iv*) Find, in terms of π , the values of θ in the interval $0 \le \theta \le 2\pi$ for which

$$2\sin^3\theta - 5\sin^2\theta + \sin\theta + 2 = 0.$$
 [4]